

12th Homework

- In this homework, we shall model chemical reactions using reaction rate equations only.
- We shall program the reaction rate equations directly in the equation window and learn to use *Modelica's* matrix notation.

- Hydrogen-Bromine Reaction
- Oxy-hydrogen Gas Reaction

Hydrogen-Bromine Reaction

- We wish to simulate the *hydrogen-bromine reaction* described during the lectures. We concentrate on mass flows only, i.e., we only model the reaction rate equations.
- We wish to plot the molar masses of the five species as functions of time.
- We shall program the reaction rate equations in the *equation window* of *Dymola*, making use of a *matrix-vector notation*, i.e., the chemical reaction network is described by the corresponding *N-matrix*.

- Although the reactions are occurring under *isothermic conditions*, we still wish to take the *Arrhenius' law* into account, and program the reaction rate constants as functions of temperature:

$$\begin{aligned}
 ak_1 &= 1.39 \cdot 10^8 \cdot \sqrt{T} \cdot \left(\frac{189243.0}{R \cdot T} \right)^{1.97} \\
 k_1 &= ak_1 \cdot \exp\left(\frac{-189243.0}{R \cdot T} \right) \\
 k_2 &= \frac{k_1}{K(T)} \\
 k_3 &= 10^{11.43} \cdot \exp\left(\frac{-82400.0}{R \cdot T} \right) \\
 k_5 &= 10^{11.97} \cdot \exp\left(\frac{-149800.0}{R \cdot T} \right) \\
 k_4 &= 0.1 \cdot k_5
 \end{aligned}$$

- where R is the gas constant ($R = 8.314 \text{ J K}^{-1} \text{ mole}^{-1}$).

- Reaction k_2 contains a temperature dependence $K(T)$ that was experimentally found:

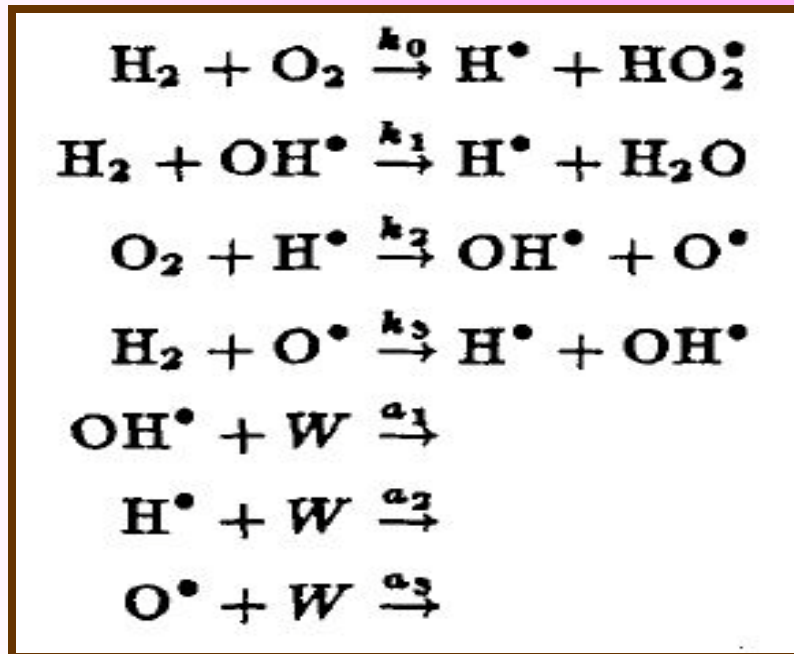
Abs. Temperature T [K]	Equilibrium Const. K [mole m ⁻³]
300.0	7.7446×10^{-29}
400.0	1.9543×10^{-20}
500.0	2.2182×10^{-16}
600.0	5.2844×10^{-12}
700.0	1.3867×10^{-9}
800.0	9.0782×10^{-8}
900.0	2.3768×10^{-6}
1000.0	3.2509×10^{-5}
1100.0	2.7861×10^{-4}
1200.0	1.6788×10^{-3}
1300.0	7.6913×10^{-3}
1400.0	2.8510×10^{-2}
1500.0	8.8716×10^{-2}
1600.0	2.4044×10^{-1}
1700.0	5.8344×10^{-1}
1800.0	1.7947
1900.0	2.6061
2000.0	4.9431

- Program $K(T)$ using a table-lookup function.

- The initial molar masses of Br_2 and H_2 are both equal to 0.0075 . The total reaction volume is $V = 0.001 \text{ m}^3$. The temperature is $T = 800 \text{ K}$.
- Simulate the system during 5000 seconds . You need to reduce the tolerance value for the *DASSL integration algorithm* to 10^{-10} .
- Plot on one graph the molar masses of Br_2 , H_2 , and HBr during the first 0.1 seconds .
- Plot on a second graph the molar mass of H^\bullet during the first 0.2 seconds .
- Plot on a third graph the molar mass of Br^\bullet during the first 0.3 seconds .

Oxy-hydrogen Gas Reaction

- When oxygen and hydrogen gases are mixed in similar proportions, a spark can bring the mixture to explosion. The process can be described by the following set of step reactions:



W stands for the wall. At the wall, the unstable atoms H^\bullet and O^\bullet , as well as the unstable radical OH^\bullet can be absorbed. The absorption rates are proportional to the molar masses of the absorbed species:

$$v_{\text{OH}^\bullet} = -a_1 \cdot n_{\text{OH}^\bullet}$$

- The reaction rate constants at the given temperature are as follows:

$$k_0 = 60.0$$

$$k_1 = 2.3 \cdot 10^{11}$$

$$k_2 = 4.02 \cdot 10^9$$

$$k_3 = 2.82 \cdot 10^{12}$$

$$a_1 = 920.0$$

$$a_2 = 80.0$$

$$a_3 = 920.0$$

Model the system in the *Dymola equation window* using a matrix-vector notation.

Simulate the system during 0.1 seconds. The initial conditions are $n_{\text{H}_2} = 10^{-7}$, and $n_{\text{O}_2} = 0.5 \cdot 10^{-7}$. The reaction volume is $V = 1.0 \text{ m}^3$.

You need to reduce the tolerance value of the *DASSL integration algorithm* to 10^{-17} .

- Plot the molar masses of H_2 , O_2 , and H_2O on one plot. Plot the molar masses of the other four species on separate plots.

References

- Tiller, M.M. (2001), *Introduction to Physical Modeling with Modelica*, Kluwer Academic Publishers, Chapter 6.5: Language Fundamentals.