

3D Mechanics

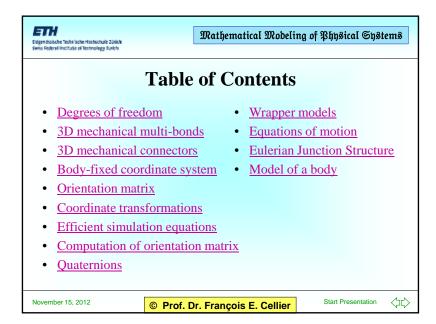
- We shall now look at a second application of multi-bond graphs: *3D mechanics*.
- 3D mechanical models look superficially just like planar mechanical models. There are additional types of joints, but other than that, there seem to be few surprises.
- Yet, the seemingly similar appearance is deceiving. There are a substantial number of complications that the modeler has to cope with when dealing with 3D mechanics. These are the subject of this lecture.

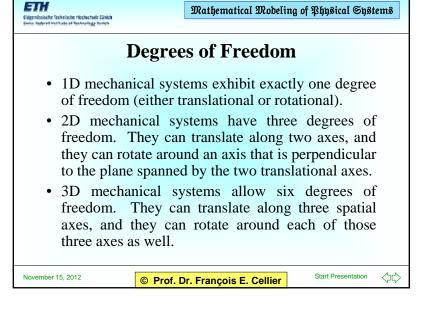
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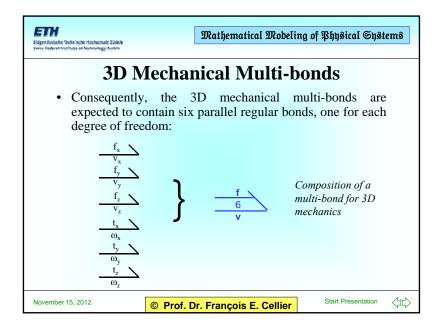
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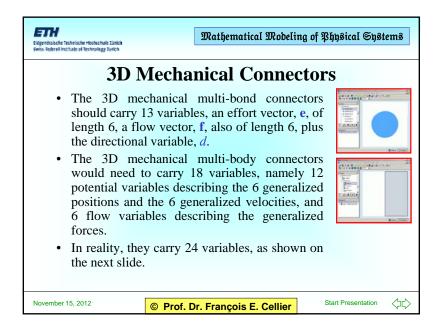
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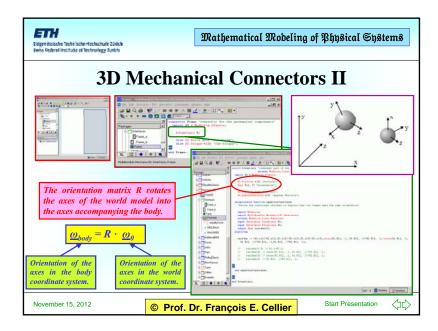


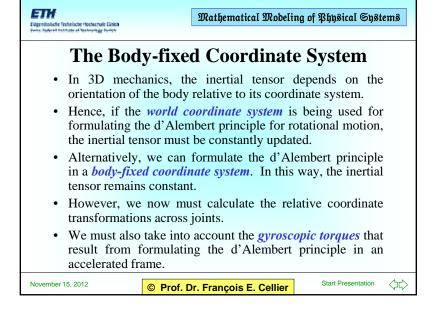


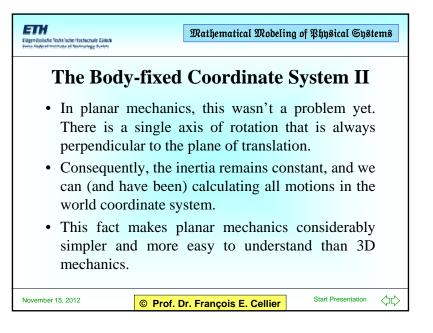


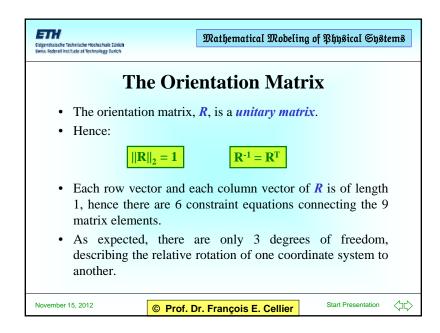


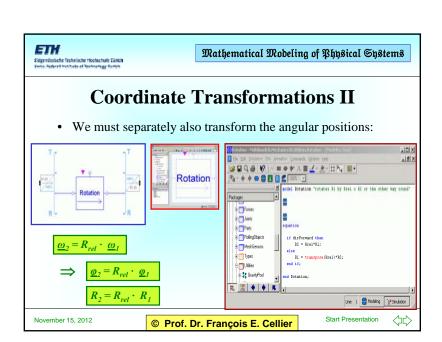


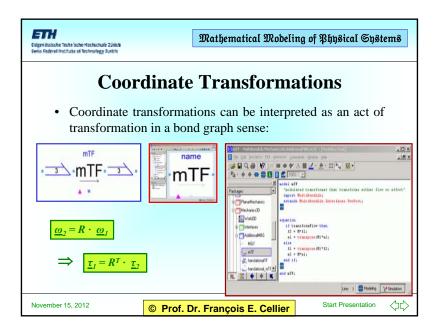


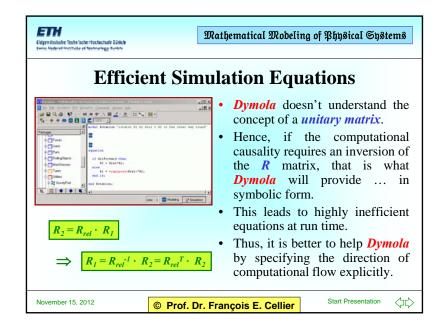


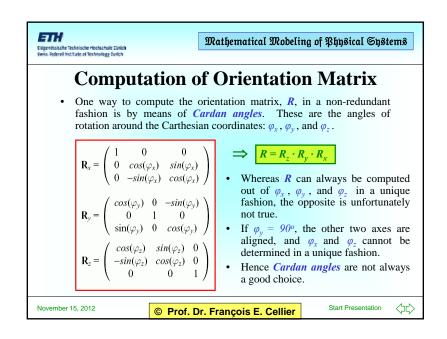


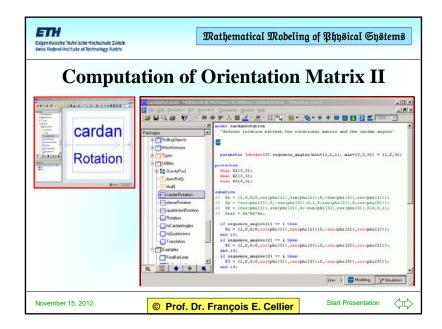


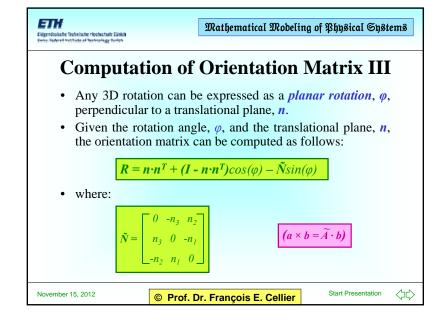


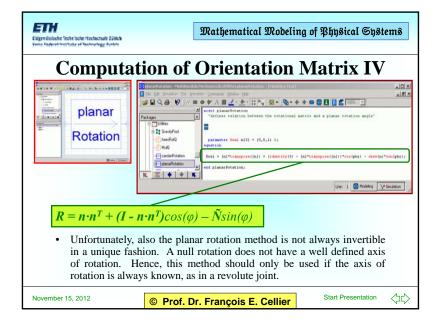














Quaternions

- A redundant way of describing orientation that works in all situations is by means of *quaternions*.
- Quaternions are a four-dimensional extension to complex numbers:

$$Q = c + ui + vj + wk = c + u$$

 Quaternions are characterized by the three imaginary components, i, j, and k that satisfy the following computational rules:

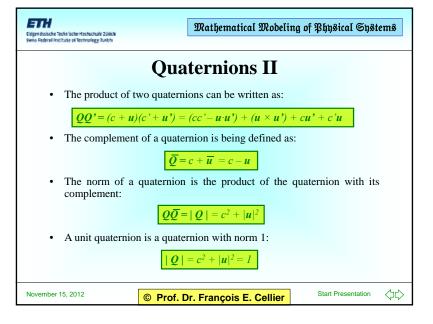
$$ij = k;$$
 $ji = -k;$ $i^2 = -1$
 $jk = i;$ $kj = -i;$ $j^2 = -1$
 $ki = j;$ $ik = -j;$ $k^2 = -1$

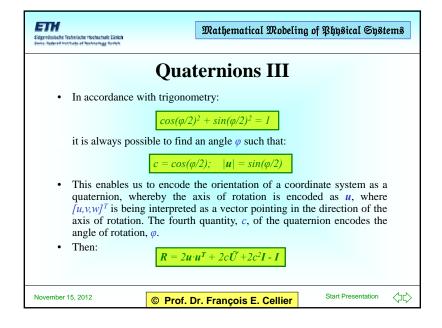
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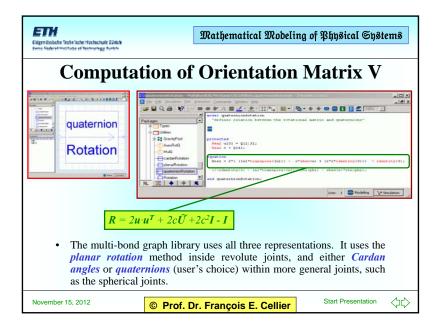
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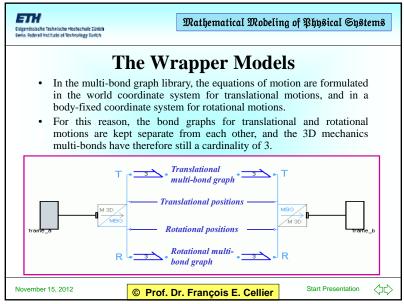
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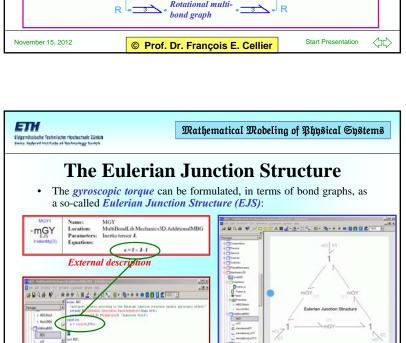












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Bond graph description

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Multi-bond graph implementation

November 15, 2012

