Numerical Simulation of Dynamic Systems: Hw2 - Problem

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Homework 2 - Problem

Marginal Stability

[H2.1] Marginal Stability

Given the following linear time-invariant continuous-time system:

$$\dot{\mathbf{x}} = \begin{pmatrix} 1250 & -25113 & -60050 & -42647 & -23999 \\ 500 & -10068 & -24057 & -17092 & -9613 \\ 250 & -5060 & -12079 & -8586 & -4826 \\ -750 & 15101 & 36086 & 25637 & 14420 \\ 250 & -4963 & -11896 & -8438 & -4756 \end{pmatrix} \cdot \mathbf{x} + \begin{pmatrix} 5 \\ 2 \\ 1 \\ -3 \\ 1 \end{pmatrix} \cdot \mathbf{u}$$

$$\mathbf{y} = \begin{pmatrix} -1 & 26 & 59 & 43 & 23 \end{pmatrix} \cdot \mathbf{x}$$

with initial conditions:

$$\mathbf{x_0} = \begin{pmatrix} 1 \\ -2 \\ 3 \\ -4 \\ 5 \end{pmatrix}$$

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Marginal Stability

[H2.1] Marginal Stability II

Determine the step size, h_{marg} , for which FE will give marginally stable results.

Simulate the system across 10 seconds of simulated time with step input using the FE algorithm with the following step sizes:

- 1. $h = 0.1 \cdot h_{\text{marg}}$,
- 2. $h = 0.95 \cdot h_{\text{marg}}$,
- 3. $h = h_{\text{marg}}$,
- 4. $h = 1.05 \cdot h_{\text{marg}}$, and
- 5. $h = 2 \cdot h_{\text{marg}}$.

Discuss the results.

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Stability Domain

[H2.5] Stability Domain

For the *predictor-corrector FE-BE method*, find the stability domains if:

- 1. no corrector is used.
- 2. one corrector is used,
- 3. two correctors are used,
- 4. three correctors are used, and
- 5. four correctors are used.

Plot the five stability domains on top of each other, and discuss the results.