Numerical Simulation of Dynamic Systems: Hw4 - Problem

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Homework 4 - Problem

BI4/50.45 Integration

[H3.15] Backinterpolation With Step-Size Control II

However, if $\varepsilon_{\rm rel} > 10^{-4}$, we reject the step at once, i.e., we never even proceed to the implicit semi-step, and compute a new step size in accordance with the same equation as during the first step.

If a step was repeated, the step size for the immediately following next step is also computed according to that equation.

Apply this step-size control algorithm to the same problem as before, and determine the largest global relative error by comparing the solution with the analytical solution of this linear time-invariant system. Numerical Simulation of Dynamic Systems: Hw4 - Problem

BI4/50.45 Integration

[H3.15] Backinterpolation With Step-Size Control

We want to repeat Hw.[H3.14] once more, this time using a step-size controlled algorithm. The step-size control to be used is the following. On the *explicit semi-step*, compute now both correctors, and find ε_{rel} according to the formula:

$$\varepsilon_{\mathrm{rel}} = \frac{\|\mathbf{x}_1 - \mathbf{x}_2\|_{\infty}}{\max(\|\mathbf{x}_1\|_2, \|\mathbf{x}_2\|_2, \delta)}$$

If $\varepsilon_{\rm rel} \le 10^{-4},$ use the Gustafsson algorithm to compute the step size to be used in the next step:

$$b_{\mathrm{new}} = \left(\frac{0.8 \cdot 10^{-4}}{\varepsilon_{\mathrm{rel}_{\mathrm{now}}}}\right)^{0.06} \cdot \left(\frac{\varepsilon_{\mathrm{rel}_{\mathrm{last}}}}{\varepsilon_{\mathrm{rel}_{\mathrm{now}}}}\right)^{0.08} \cdot h_{\mathrm{old}}$$

except during the first step, when we use:

$$h_{
m new} = \left(rac{0.8\cdot 10^{-4}}{arepsilon_{
m rel_now}}
ight)^{0.2}\cdot h_{
m old}$$

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Order Star

[H3.19] Order Star

Find the *damping order star* for $BI4/5_{0.45}$, and plot it together with the pole and zero locations. Compare with the damping order star of BI4 that was shown in class.

Find the *frequency order star* for $B14/5_{0.45}$, and plot it together with the pole and zero locations. Compare with the frequency order star B14 that was shown in class.

Finally, compute and plot the order star accuracy domain of this method.

For this problem, it may be easier to use MATLAB's contour plot, than your own domain tracking routine.