

Eidgenössische Technische Hochschule Zürich

Swiss Federal Institute of Technology Zurich

Mathematical Modeling of Physical Systems


The Dymola Bond Graph Library


- In this class, we shall deal with some issues relating to the construction of the *Dymola Bond Graph Library*.
- The design principles are explained, and some further features of the *Dymola* modeling framework are shown.
- We shall introduce the concept of model wrapping as implemented in the bond graph library.
- An example of an electronic circuit simulation completes the presentation.

October 18, 2012

© Prof. Dr. François E. Cellier

Start Presentation





Eidgenössische Technische Hochschule Zürich

Swiss Federal Institute of Technology Zurich

Mathematical Modeling of Physical Systems


Table of Contents


- [Across and through variables](#)
- [Gyro-bonds](#)
- [Graphical bond-graph modeling](#)
- [Bond-graph connectors](#)
- [A-causal and causal bonds](#)
- [Junctions](#)
- [Element models](#)
- [Model wrapping](#)
- [Bond-graph electrical library](#)
- [Wrapped resistor model](#)
- [Bipolar junction transistor](#)
- [Inverter Circuit](#)

October 18, 2012

© Prof. Dr. François E. Cellier

Start Presentation





Eidgenössische Technische Hochschule Zürich

Swiss Federal Institute of Technology Zurich

Mathematical Modeling of Physical Systems


Across and Through Variables


- Dymola* offers two types of variables, the *across variables* and the *through variables*.
- In a *Dymola node*, across variables are set equal across all connections to the node, whereas through variables add up to zero.
- Consequently, if we equate *across variables* with *efforts*, and *through variables* with *flows*, *Dymola nodes* correspond exactly to the *0-junctions* of our bond graphs.

October 18, 2012

© Prof. Dr. François E. Cellier

Start Presentation





Eidgenössische Technische Hochschule Zürich

Swiss Federal Institute of Technology Zurich

Mathematical Modeling of Physical Systems

Gyro-bonds


- In my modeling book, I exploited this similarity by implementing the *bonds* as *twisted wires* (as *null-modems*).
- By requesting furthermore that:
 - ♣ 0- and 1-junctions must always toggle. No two junctions of the same gender may be connected by a bond.
 - ♣ All elements must always be attached to 0-junctions, never to 1-junctions.

both the *0-junctions* and the *1-junctions* can be implemented as *Dymola nodes*.

October 18, 2012

© Prof. Dr. François E. Cellier

Start Presentation



ETH
Eidgenössische Technische Hochschule Zürich
Swiss Federal Institute of Technology Zurich

Mathematical Modeling of Physical Systems

Gyro-bonds II

October 18, 2012

© Prof. Dr. François E. Cellier

Start Presentation

ETH
Eidgenössische Technische Hochschule Zürich
Swiss Federal Institute of Technology Zurich

Mathematical Modeling of Physical Systems

Graphical Bond Graph Modeling I

- For graphical bond-graph modeling, these additional rules may, however, be too constraining.
- For example, thermal systems often exhibit 0-junctions with many bonds attached. It must be possible to split these 0-junctions into a series of separate 0-junctions connected by bonds, so that the number of bonds attached at any one junction can be kept sufficiently small.

October 18, 2012

© Prof. Dr. François E. Cellier

Start Presentation

ETH
Eidgenössische Technische Hochschule Zürich
Swiss Federal Institute of Technology Zurich

Mathematical Modeling of Physical Systems

Graphical Bond Graph Modeling II

- For this reason, the graphical bond graph modeling of *Dymola* defines both *efforts* and *flows* as *across variables*.

- Consequently, the *junctions* will have to be programmed explicitly. They can no longer be implemented as *Dymola nodes*.

October 18, 2012

© Prof. Dr. François E. Cellier

Start Presentation

ETH
Eidgenössische Technische Hochschule Zürich
Swiss Federal Institute of Technology Zurich

Mathematical Modeling of Physical Systems

The Bond Graph Connectors I

Equation window

Icon window

- The directional variable, *d*, is a third across variable made available as part of the *bond-graph connector*, which is depicted as a *grey dot*.

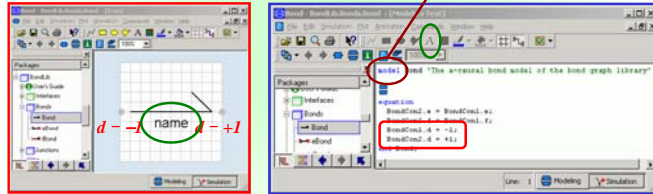
October 18, 2012

© Prof. Dr. François E. Cellier

Start Presentation

The A-Causal Bond “Model”

- The model of a bond can now be constructed by dragging two of the bond-graph connectors into the diagram window. They are named *BondCon1* and *BondCon2*.



Icon window

Equation window

Place the text “%name” in the icon window to get the name of the model displayed upon invocation.

October 18, 2012

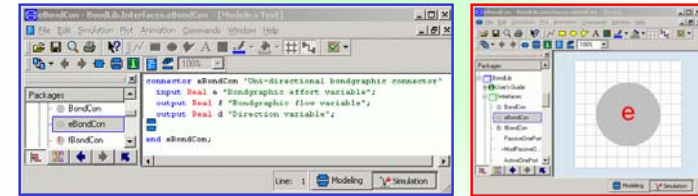
© Prof. Dr. François E. Cellier

Start Presentation



The Bond Graph Connectors II

- Dymola* variables are usually a-causal. However, they can be made causal by declaring them explicitly in a causal form.
- Two additional bond-graph connectors have been defined. The *e-connector* treats the *effort* as an *input*, and the *flow* as an *output*.



- The *f-connector* treats the *flow* as *input* and the *effort* as *output*.

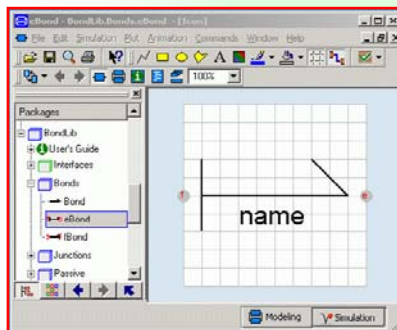
October 18, 2012

© Prof. Dr. François E. Cellier

Start Presentation



The Causal Bond “Blocks”



Using these connectors, causal bond blocks can be defined.

The *f-connector* is used at the side of the causality stroke.

The *e-connector* is used at the other side.

The causal connectors are only used in the context of the bond blocks. Everywhere else, the normal bond-graph connectors are to be used.

October 18, 2012

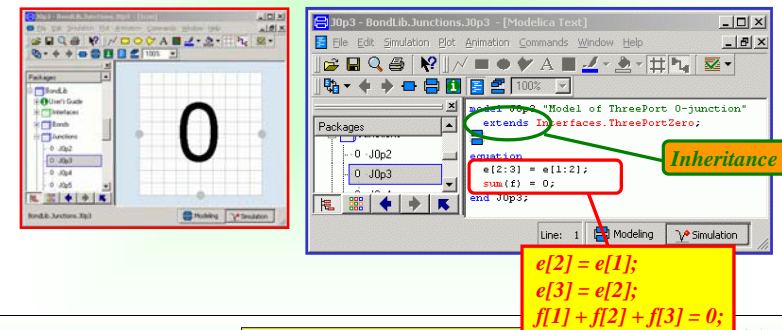
© Prof. Dr. François E. Cellier

Start Presentation



The Junctions I

- The junctions can now be programmed. Let us look at a *0-junction with three bond attachments*.




October 18, 2012

© Prof. Dr. François E. Cellier

Start Presentation

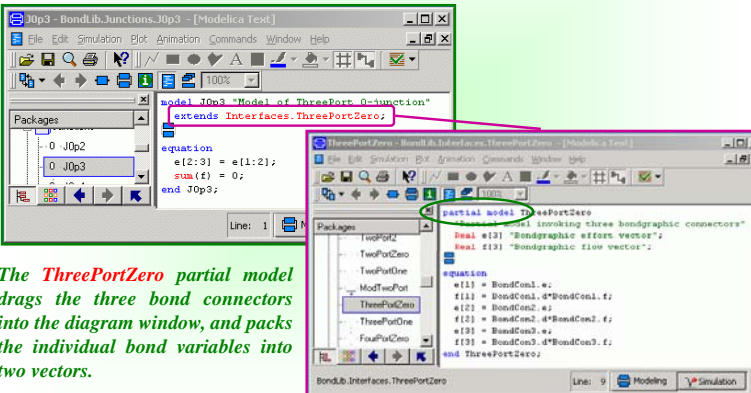





Eidgenössische Technische Hochschule Zürich
Swiss Federal Institute of Technology Zurich


Mathematical Modeling of Physical Systems

The Junctions II



*The **ThreePortZero** partial model drags the three bond connectors into the diagram window, and packs the individual bond variables into two vectors.*

October 18, 2012
© Prof. Dr. François E. Cellier
Start Presentation 

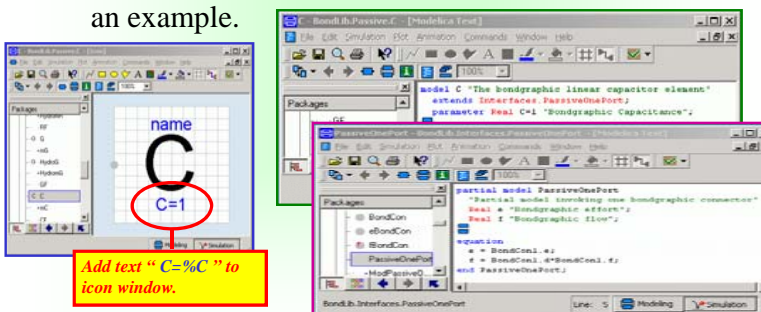


Eidgenössische Technische Hochschule Zürich
Swiss Federal Institute of Technology Zurich


Mathematical Modeling of Physical Systems


The Element Models

- Let us now look at the bond-graphic element models. The bond graph capacitor may serve as an example.



Add text "C=%C" to icon window.

October 18, 2012
© Prof. Dr. François E. Cellier
Start Presentation 





Eidgenössische Technische Hochschule Zürich
Swiss Federal Institute of Technology Zurich

Mathematical Modeling of Physical Systems

Model Wrapping

- Although it is possible to model physical systems manually down to the bond graph level, this may not always be convenient.
- The bond graph interface is the lowermost graphical interface that is still fully object-oriented.
- The interface is important as it keeps the distance between the lowermost graphical layer and the equation layer as small as possible.
- Higher level graphical layers can be built easily on top of the bond graph layer for enhanced convenience.

October 18, 2012
© Prof. Dr. François E. Cellier
Start Presentation 





Eidgenössische Technische Hochschule Zürich
Swiss Federal Institute of Technology Zurich

Mathematical Modeling of Physical Systems

The Bond Graph Electrical Library

- It is possible to wrap any other object-oriented graphical modeling paradigm around the bond graph methodology.
- This was done with the analog electrical library that forms part of the standard library of Modelica.
- A new analog electrical library was created as part of the bond graph library.
- In this new library, the bottom layer graphical models were wrapped around a yet lower level bond graph layer.

October 18, 2012
© Prof. Dr. François E. Cellier
Start Presentation 

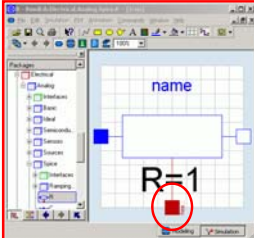


Eidgenössische Technische Hochschule Zürich

Swiss Federal Institute of Technology Zürich

Mathematical Modeling of Physical Systems

The Wrapped Resistor Model



Icon window

The *wrapper models* convert the connectors between the three domains: electrical, thermal, and bond graph.

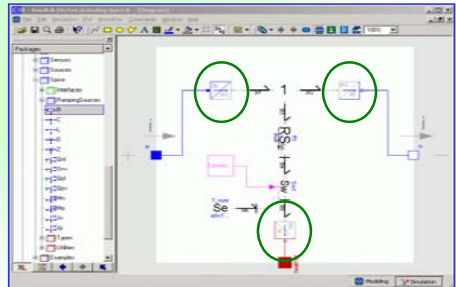



Diagram window

October 18, 2012

© Prof. Dr. François E. Cellier

Start Presentation

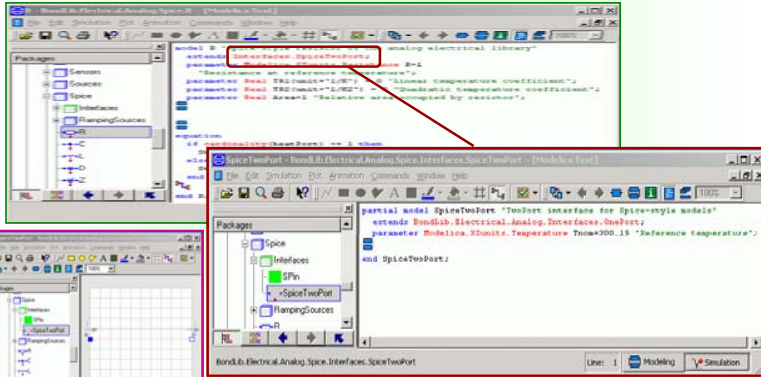


Eidgenössische Technische Hochschule Zürich

Swiss Federal Institute of Technology Zürich


Mathematical Modeling of Physical Systems

The Wrapped Resistor Model II



© Prof. Dr. François E. Cellier

Start Presentation

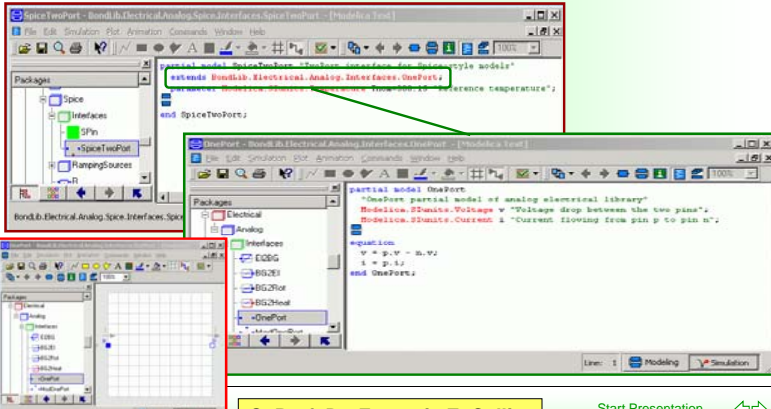


Eidgenössische Technische Hochschule Zürich

Swiss Federal Institute of Technology Zürich


Mathematical Modeling of Physical Systems

The Wrapped Resistor Model III



© Prof. Dr. François E. Cellier

Start Presentation



Eidgenössische Technische Hochschule Zürich

Swiss Federal Institute of Technology Zürich

Mathematical Modeling of Physical Systems

The Wrapped Resistor Model IV

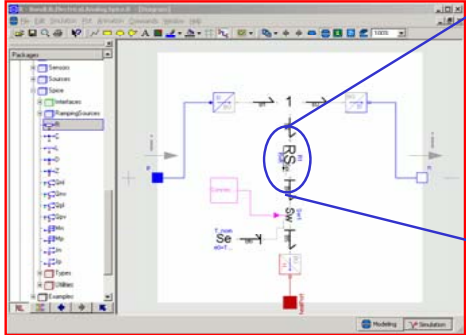
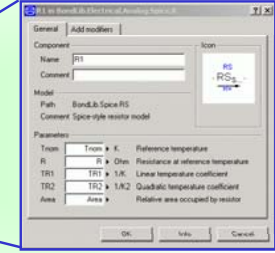


Diagram window



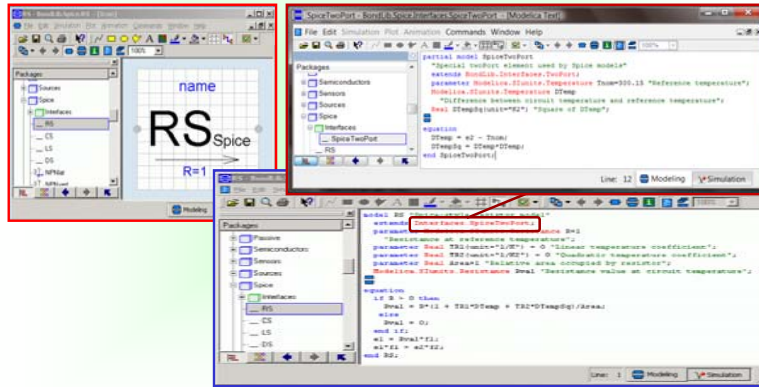
Parameter window

October 18, 2012

© Prof. Dr. François E. Cellier

Start Presentation

The Wrapped Resistor Model V



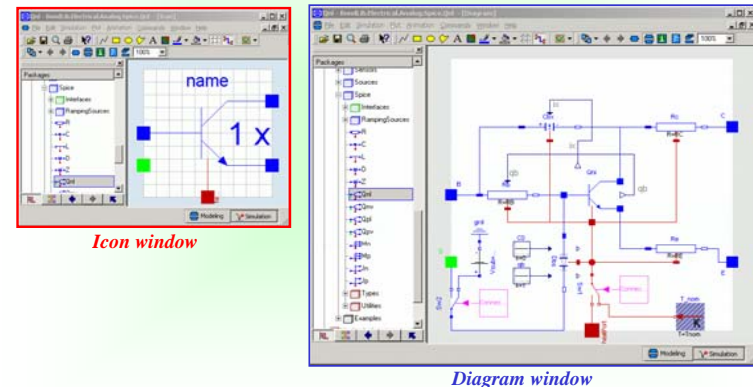
October 18, 2012

© Prof. Dr. François E. Cellier

Start Presentation



The Bipolar Junction Transistor



Icon window

Diagram window

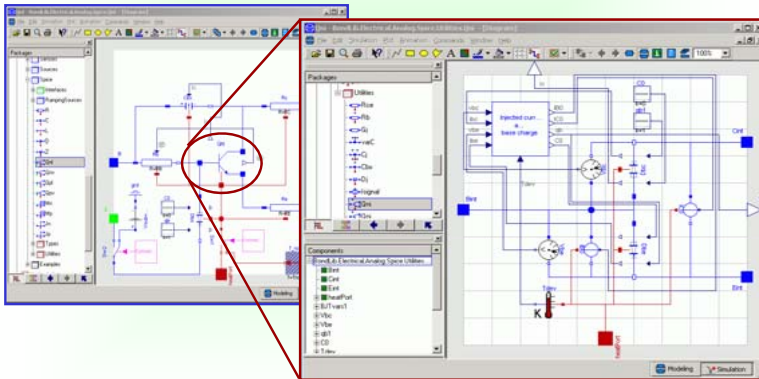
October 18, 2012

© Prof. Dr. François E. Cellier

Start Presentation



The Bipolar Junction Transistor II



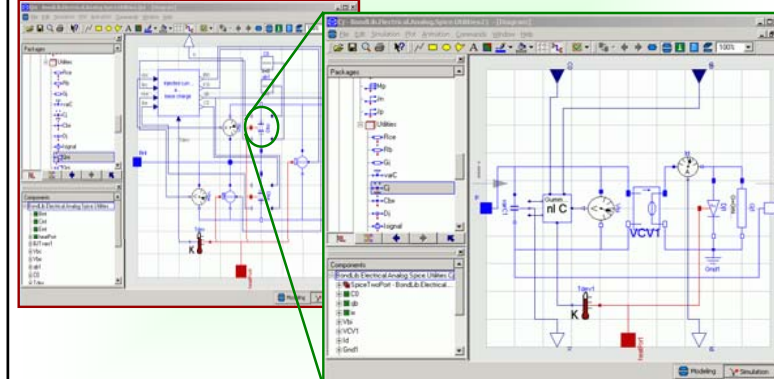
October 18, 2012

© Prof. Dr. François E. Cellier

Start Presentation



The Bipolar Junction Transistor III



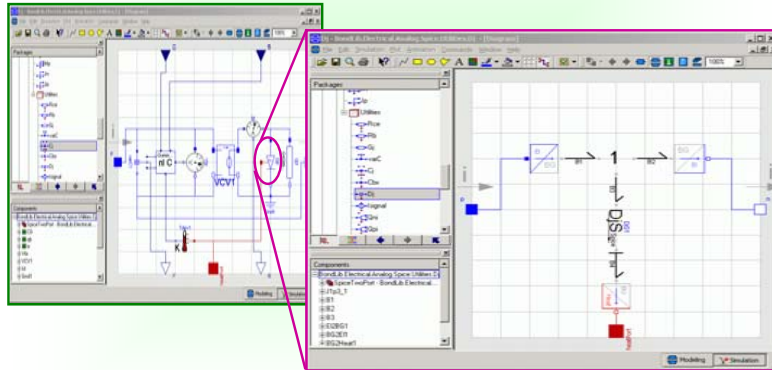
October 18, 2012

© Prof. Dr. François E. Cellier

Start Presentation



The Bipolar Junction Transistor IV



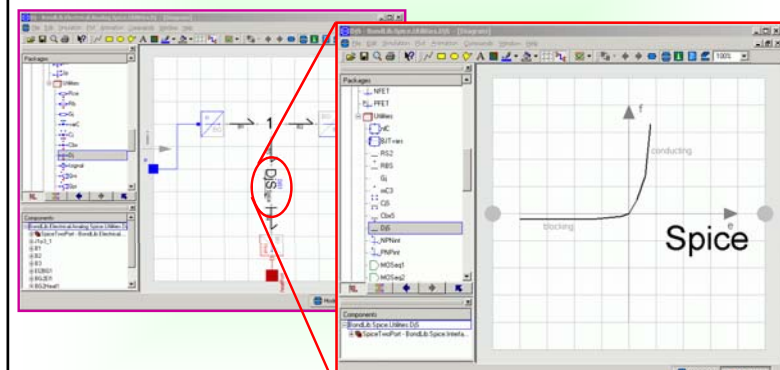
October 18, 2012

© Prof. Dr. François E. Cellier

Start Presentation



The Bipolar Junction Transistor V



October 18, 2012

© Prof. Dr. François E. Cellier

Start Presentation



The Bipolar Junction Transistor VI

```

model BJT "Spice-style junction diode model for bipolar transistor"
extends InterfaceSpiceModel;
constant Modelica.SIunits.Entropy kModelica.Constants.k
  "Boltzmann's constant";
constant Modelica.SIunits.ElectricCharge q1.6021892e-19 "Electron charge";
constant Real GapC1=7.028e-4 "First bandgap correction factor Silicon";
constant Real GapC2=1.08e-5 "Second bandgap correction factor Silicon";
parameter Modelica.SIunits.Current IS=1e-16
  "Saturation current at reference temperature";
parameter Modelica.SIunits.Voltage RS=1.16
  "Energy gap for temperature effect on saturation current";
parameter Real N1=1 "Current emission coefficient";
parameter Real XT1=1 "Saturation current temperature exponent";
parameter Real Area=1 "Relative area occupied by diode";
parameter Integer Level=1
  "Transistor modeling level (Barr-Hall = 1; Gummel-Poon = 2)";
parameter Real EMin=100 "if z = EMin, the exp() function is linearized";
parameter Real EMax=40 "if z = EMax, the exp() function is linearized";
Modelica.SIunits.Voltage VT "Thermal voltage";
Modelica.SIunits.Current ISval "Saturation current at device temperature";
Modelica.SIunits.Energy RSval "Activation energy at device temperature";

protected
  parameter Real EMin = exp(RMin);
  parameter Real EMax = exp(RMax);
  Real XTexp "Temperature quotient";
  Real z;

equation
  /* Compute thermal voltage as function of temperature */
  VT = k*T/q;
  z = q1/(k*T);

  /* Compute temperature dependence of saturation current */
  XTexp = z/TS;
  RSval = RS - GapC1*z/2*(z + GapC2);
  ISval = IS*exp(XTexp - 1)*ISval/VT + XT1*ln(XTexp);

  /* Compute diode characteristic */
  if Level==2 then
    /* Gummel-Poon model */
    z1 = ISval*area*(if z < EMin then EMin*(z - EMin + 1) - 1 else
      if z > EMax then EMax*(z - EMax + 1) - 1 else exp(z) - 1);
  else
    /* Barr-Hall model */
    z1 = ISval*(if z < EMin then EMin*(z - EMin + 1) - 1 else
      if z > EMax then EMax*(z - EMax + 1) - 1 else exp(z) - 1);
  end if;

  /* Compute heat flow */
  z2 = 0;

end BJT;

```

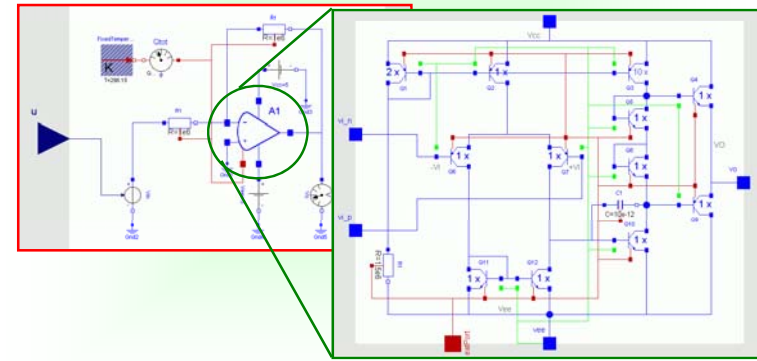
October 18, 2012

© Prof. Dr. François E. Cellier

Start Presentation



Inverter Circuit



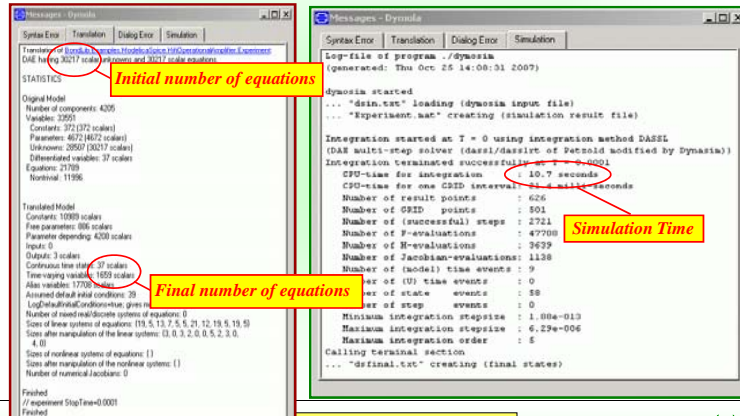
October 18, 2012

© Prof. Dr. François E. Cellier

Start Presentation



Inverter Circuit II

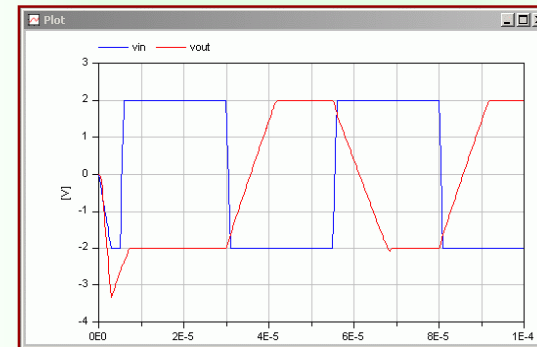


Dr. François E. Cellier

Start Presentation



Simulation Results



October 18, 2012

© Prof. Dr. François E. Cellier

[Start Presentation](#)



References

- Cellier, F.E. and R.T. McBride (2003), “Object-oriented modeling of complex physical systems using the Dymola bond-graph library,” *Proc. ICBGM’03, Intl. Conf. Bond Graph Modeling and Simulation*, Orlando, FL, pp. 157-162.
- Cellier, F.E. and A. Nebot (2005), “The Modelica Bond Graph Library,” *Proc. 4th Intl. Modelica Conference*, Hamburg, Germany, Vol.1, pp. 57-65.
- Cellier, F.E., C. Clauß, and A. Urquía (2007), “Electronic Circuit Modeling and Simulation in Modelica,” *Proc. 6th Eurosim Congress*, Ljubljana, Slovenia, Vol.2, pp. 1-10.
- Cellier, F.E. (2007), *The Dymola Bond-Graph Library*, Version 2.3.

October 18, 2012

© Prof. Dr. François E. Cellier

Start Presentation

