An optimization framework for simulation and kinematic control of Constrained Collaborative Mobile Agents (CCMA) system

Nitish Kumar*, Stelian Coros

Abstract—We present a concept of constrained collaborative mobile agents (CCMA) system, which consists of multiple wheeled mobile agents constrained by a passive kinematic chain. This mobile robotic system is modular in nature, the passive kinematic chain can be easily replaced with different designs and morphologies for different functions and task adaptability. Depending solely on the actuation of the mobile agents, this mobile robotic system can manipulate or position an end-effector. However, the complexity of the system due to presence of several mobile agents, passivity of the kinematic chain and the nature of the constrained collaborative manipulation requires development of an optimization framework. We therefore present an optimization framework for forward simulation and kinematic control of this system. With this optimization framework, the number of deployed mobile agents, actuation schemes, the design and morphology of the passive kinematic chain can be easily changed, which reinforces the modularity and collaborative aspects of the mobile robotic system. We present results, in simulation, for spatial 4-DOF to 6-DOF CCMA system examples. Finally, we present experimental quantitative results for two different fabricated 4-DOF prototypes, which demonstrate different actuation schemes, control and collaborative manipulation of an end-effector.

Index Terms—Collaborative robots, Multi-robot systems, Mobile manipulation, Simulation, modeling and control

I. INTRODUCTION

From structured warehouses to unstructured environments such as construction sites, agricultural fields, research into large scale mobile robotics systems is fuelled by demands for increased mobility, task adaptability while able to perform various functions. Most of the mobile robotic systems have a monolithic hardware architecture consisting of fully actuated serial manipulator/s mounted on a single mobile base. Due to the monolithic and inflexible hardware architecture, current systems miss the potential advantages of task-adaptability, shared collaborative manipulation brought upon by a more modular, lightweight architecture.

Therefore, we present an alternate concept for a modular, collaborative and task-adaptable mobile robotic system consisting of multiple mobile bases (Fig. 1). Our goal is to develop a unified system that allows us to explore 1) collaborative manipulation using teams of mobile robots, and 2) reconfigurable manipulators that use simple robotic systems as building blocks. CCMA system is modular in nature such that the number of mobile bases, actuation schemes and the design, morphology of the passive kinematic chain can be easily changed in hardware. The task of a single heavy mobile base is substituted by collaboration between and shared manipulation by several light weight mobile bases. Fully actuated serial manipulator/s are substituted by a fully constrained passive closed-loop kinematic mechanism.

The above mentioned flexibilities in the hardware architecture can only be realized in practice, if a corresponding flexible software framework is developed for easier and faster evaluation of vast design and actuation space that CCMA system presents. Therefore, we develop and present an optimization framework for simulation and control of CCMA system, which allows for easy and fast change in actuation schemes, number of mobile agents, design and morphology of the passive kinematic chain. We evaluate this optimization framework on different prototypes of the CCMA system, in simulation and experiments, for end-effector manipulation and positioning tasks.

A. Related Work on System Architecture

In the field of construction robotics or robotics in architecture, process specific digital fabrication techniques such as robotic brickwork [1], robotic formwork [2] increasingly make use of more generic mobile robotic systems [3]. These mobile robotic systems typically include a fully actuated
industrial manipulator mounted on a single mobile base which can be wheeled or tracked [4], [5].

There are several reports of different modular hardware architectures which use multiple mobile agents to collaboratively perform a task. For e.g., multiple flying agents were used for building an architecture scale installation in this work [6]. However, flight based agents lack the rigidity and stiffness required for more demanding manipulation tasks. Another approach consists in using wheeled mobile agents to collaboratively manipulate an object which is suspended through several cables [7], [8]. Cable driven object manipulation has the capability to provide the rigidity, stiffness and higher payloads. However to fulfill these requirements, the topology of the cables encircles the object being manipulated, thereby reducing the available workspace around the end-effector.

Hardware system architecture, where a passive kinematic chain with rigid links is connected to multiple mobile agents (CCMA), has the potential to replace conventional large scale mobile robotic systems for a variety of tasks. Owing to higher rigidity of the links and flexible arrangement of the kinematic chain around the end-effector, such systems would allow for open workspace around the end-effector to carry out process-specific tasks. Few prototypes with this system architecture have been previously reported in the work [9], [10], [11]. However, morphology of the passive kinematic chain was limited to 6-DOF, with a single link with two passive joints connecting the end-effector to each mobile base. Choice of the actuation scheme was conservative and a fixed number of mobile agents were used. This misses a big potential advantage, where over-actuation along with use of multiple mobile agents and different actuation schemes can be exploited to enhance the system performance.

In the current work, we present a generalized concept for this hardware system architecture. Our work accommodates a far richer design space for the passive kinematic chains and diverse actuation schemes for multiple mobile agents.

B. Related Work on Simulation, Modeling and Kinematic Control Techniques

An overview of kinematic modeling techniques for robotic systems with closed loop kinematic chains can be found in [12], [13], [14], [15]. These techniques result in models in the form of \( \mathbf{J}_x \cdot \mathbf{X} = \mathbf{J}_q \cdot \mathbf{q} \), either obtained through differentiating forward position models of the form \( \mathbf{X} = f(\mathbf{q}) \) or directly through screw theory [16] based generation of twist and wrench systems [12], [15]. \( \mathbf{X} \) represents the end-effector variables and \( \mathbf{q} \) contains the independent active control variables, such as motor angles. These two \( \mathbf{J}_x \) and \( \mathbf{J}_q \) matrices form the essential components for numerical techniques either for solving forward kinematics problems (simulation) or inverse kinematics problems [17] (control) through the relation \( \mathbf{J}_x \cdot \delta \mathbf{X} = \mathbf{J}_q \cdot \delta \mathbf{q} \).

Even though the above numerical methods and modeling techniques lead to fast computation of forward and inverse kinematic solutions, the implementation of the Jacobian matrices \( \mathbf{J}_x \) and \( \mathbf{J}_q \) is still tailored to individual robots with manual error prone time consuming steps, like differentiation of robot specific forward position models, elimination steps for closed loop kinematic chains. However, optimization-based simulation and control scheme proposed in the current work is very generic, and it is readily applicable to any instance of a CCMA system without requiring any new code to be written, or any new Jacobian terms to be derived. We have developed a modular simulation and control scheme to accompany the novel concept of modular CCMA systems.

In the current work, rigid body kinematics is modeled on a constraint based formulation presented in the paper [18], [19], which abstracts a rigid body robotic system to a collection of rigid bodies connected with kinematic constraints imposed by the joints and actuators. We extend this modeling framework by including additional constraints for the mobile agents acting as actuators. Due to this abstraction, no separate specific implementation is needed for different actuation schemes, number of mobile agents and different designs, morphologies of the passive kinematic chain.

For the simulation (forward kinematics) of the CCMA system, we calculate the derivatives of the kinematic constraints including those imposed by the actuation of mobile agents analytically. Moreover, we calculate the derivatives of the tasks, formulated as objective functions, with respect to control parameters of the CCMA system for solving the kinematic control problem (inverse kinematics). These derivatives are required for the gradient-based methods (e.g. L-BFGS, Gauss-Newton). For analytical formulation of the derivatives, we utilize the first order sensitivity analysis techniques [20], [21], [22]. The analytical derivation of the derivatives, as compared to using finite differences, allows for real time computation of both forward kinematics (simulation) and inverse kinematics (kinematic control) of the CCMA system, despite being system independent.

C. Contributions

Our long term goal is to leverage the advantages brought by combining robotic mobility and manipulation capabilities. To this end, in this paper we show that driven by appropriate control systems, very simple robots equipped with very simple manipulators can be quite dexterous. The mobile manipulation systems, we study in this work, have much greater workspace and reach than stationary robots. They are very lightweight, and they can easily be reconfigured to fit the needs of different tasks. In this paper, we make following contributions:

- A general concept for constrained collaborative mobile agents (CCMA), in which an end-effector is connected via a passive kinematic chain to multiple mobile agents.
- Varying topology of the kinematic chain and actuation schemes of the mobile agents for task adaptability.
- A unified optimization framework for simulation and kinematic control of CCMA systems, independent of design, morphology of the passive kinematic chain and actuation schemes, number of mobile agents.
- Two prototypes demonstrating the optimization driven kinematic control of the CCMA system in experiments.
II. CONSTRAINED COLLABORATIVE MOBILE AGENTS
SYSTEM DESCRIPTION AND MODELING

Fig. 1 illustrates the concept of CCMA system. It consists of a passive kinematic chain connecting the end-effector (black polygon) to a number of omni-directional mobile bases either through a fixed connection or an extra revolute joint (in black color) at the mobile base. The mobile agents form the only actuators in the system to control the end-effector. Omni-directional mobile base has 3-DOF, each of which is used as an actuator. The extra passive black revolute joint is along the rotation axis of the omni-directional robot. Because of this revolute joint, actuation due to rotation of the omni-directional base has no effect on the end-effector motion. This reduces the effective control variables in each omni-directional robot to 2 (reduced actuation scheme) from 3 (complete actuation scheme). The CCMA example in Fig. 2(a) has black revolute joints, therefore it utilizes effective 6 control variables to manipulate the end-effector. Whereas the CCMA example in Fig. 2(b) has a fixed connection (no black revolute joint), therefore it utilizes effective 9 control variables. The number of mobile bases (6 in Fig. 1) 3 in Fig. 2 and Fig 3 can be varied in the CCMA system. Moreover, design and morphology of the passive kinematic chain can be varied in the CCMA system, as shown with different design and morphologies in Figs. 1, 2 and 3 for different CCMA system examples.

A. Notation and preliminaries

- $n_b$: the total number of the rigid bodies in the CCMA system inclusive of passive kinematic chain and all the mobile bases.
- $n_m$: the number of planar mobile robots.
- $s$: state vector of the system, which has a size of $6 \cdot n_b$.
- $u$: the size of control vector $u$ is $3 \cdot n_m$. For reduced actuation scheme, the control variable corresponding to orientation of the mobile base can be arbitrarily fixed leaving effective 2 control parameters for a single mobile base.

The CCMA system consists of rigid bodies connected with kinematic constraints. Without any kinematic constraints, each rigid body $i$ has 6-DOF which is described by its state $s_i = [\gamma_i, \beta_i, \alpha_i, T_i]^T$, consisting of three Euler angles and translation vector $T_i = [x_i, y_i, z_i]^T$ from global reference frame to rigid body local co-ordinate system. Thus any point $p_i$ or free vector $v_i$ expressed in local co-ordinate system of a rigid body $i$ can be converted to global world co-ordinates as $p_i = R_{\gamma_i} \cdot R_{\beta_i} \cdot R_{\alpha_i} \cdot p_i + T_i$ or $v_i = R_{\gamma_i} \cdot R_{\beta_i} \cdot R_{\alpha_i} \cdot v_i$. $R$ is an elementary $3 \times 3$ rotation matrix.

The kinematic constraints are imposed between rigid bodies $i$ and $j$, which are collected in a vector of constraints $C$. These kinematic constraints are imposed by the passive kinematic connections in form of joints in the passive kinematic chain and due to actuation of the mobile agents. For example, we illustrate how to formulate the kinematic constraints due to a revolute and a spherical kinematic connection. Furthermore, we also describe how to formulate the kinematic constraints resulting from actuation of the omni-directional mobile bases.

1) Revolute/Spherical joint: Let $v_i(\bar{v}_i)$ be a free vector passing through a point $p_i(\bar{p}_i)$ on a rigid body $i$ and similarly we define terms for another rigid body $j$. Then a revolute joint connection between rigid body $i$ and $j$ imposes the kinematic constraint $C_{ij}^{rev} = [(p_j(\bar{p}_j) - p_i(\bar{p}_i))^T (v_j(\bar{v}_j) - v_i(\bar{v}_i))^T]^T$. $C_{ij}^{rev}$ consists of 6 scalar constraints, first and second 3 scalar constraints measure distance between each component of two points and two vectors, respectively. When these 6 scalar constraints have zero value, they define the rotation axis of the revolute joint passing through coincident points of two rigid bodies. It should be noted that there are effectively only 5 independent scalar constraints which allow 1-DOF for a revolute joint connection. A spherical joint connection imposes the kinematic constraint $C_{ij}^{sph} = (p_j(\bar{p}_j) - p_i(\bar{p}_i))^T$. $C_{ij}^{sph}$ consists of 3 scalar constraints. When these three scalar constraints have zero value, a spherical joint connection is created with a coincident center of rotation. There are effectively 3 independent scalar constraints which allow 3-DOF between the rigid bodies $i$ and $j$ for a spherical joint connection. For more details, please refer to [18], [19].
2) Omnidirectional mobile bases: Each mobile base $k = 0, 1, \ldots, n_m - 1$ is also counted as a rigid body with state $s_k^m = [\gamma_k^m \beta_k^m \alpha_k^m \mathbf{x}_k^m \mathbf{y}_k^m \mathbf{z}_k^m]^T$. Let $\mathbf{v}_k^m$ be a unit vector attached to planar mobile base, which is perpendicular to its plane. For a world reference frame $\mathbf{O}_g, \mathbf{x}_g, \mathbf{y}_g, \mathbf{z}_g$ $\mathbf{x}_g$, $\mathbf{y}_g$ and $\mathbf{z}_g$ are three unit vectors and $\mathbf{O}_g = [0 \ 0 \ 0]^T$. For each mobile base, we add kinematic constraints $C_{k}^{\text{planar}} = [z_k^m \cdot (v_k^m \cdot v_k^m) - z_k^m]^T$ which correspond to the planar constraint on the mobile robot. This planar constraint restricts translation along $\mathbf{z}_g$ and rotation about $\mathbf{x}_g$ and $\mathbf{y}_g$. We further add motor constraints assuming motorized prismatic actuators along $\mathbf{x}_g$, $C_{k}^{mx} = x_g^m - u[3 \cdot k]$, and along $\mathbf{y}_g$, $C_{k}^{my} = y_g^m - u[3 \cdot k + 1]$. Let $\mathbf{v}_k^p = [1 \ 0 \ 0]^T$ be a unit vector in the plane of the mobile robot and $\theta = u[3 \cdot k + 2]$ be angle between $\mathbf{v}_k^p$ and $\mathbf{x}_g$ about axis $\mathbf{z}_g$. We further add motor constraints assuming motorized rotary actuator about axis $\mathbf{z}_g$, $C_{k}^{mx} = C_{k}^{my} = R_{g}^{p} \cdot (R_{g} \cdot \mathbf{v}_k^p) - x_g$. For the reduced vector equations of constraints $C$, the vector $\hat{s}$ includes all these constraints output by each passive joint (revolute, prismatic, spherical, universal) between the two rigid bodies, motor constraints obtained by fixing the value of actuator in the motorized joint between the two rigid bodies. It should be noted that the vector of constraints $C$ is both a function of $s$ and $u$.

III. Optimization framework for simulation and kinematic control of CCMA system

A. Simulation of the CCMA system

For simulation of the CCMA system, we solve an optimization problem where we minimize an energy $E(s, u)$ which is a function of state $s$ and control variables in $u$. The vector $C$ contains all the kinematic constraints including those imposed by the passive kinematic chain and the actuation of multiple mobile and control variables.

$$\hat{s} = \min_{s(u)} E(s, u) = \frac{1}{2} C(s, u)^T C(s, u) \quad (1)$$

This allows us to simulate the CCMA system and solve the forward kinematics problem which is to find the complete state $\hat{s}$, including the designated end-effector state, $X_{EE}$, when the control vector $u$ is given as input. We calculate analytically the first and second order derivatives $\frac{dE}{ds}$ and $\frac{dE}{du}$ and utilize standard Newton Raphson method to solve this minimization problem in iterative manner as follows:

$$s_{i+1} = s_i - \left(\frac{d^2 E}{ds^2}\right)^{-1} \left|_{s=s_i} \frac{dE}{ds}\right|_{s=s_i}$$

Since, $C$ and the resulting constraint energy term $E$ are abstracted to the level of type of joints or what type of actuators are used, the analytical derivation of the $C_{k}^{\text{planar}}$ is system independent. This allows us to plug and play different design, topologies of the passive kinematic chain and different actuation schemes, number of mobile agents, in the CCMA system.

B. Kinematic control of the CCMA system

In order to solve the kinematic control problem, which is to find $u$ for desired end-effector state $X_{EE}$, we solve the optimization problem Eqn. 2. The minimization in Eqn. 1 only ensures that the gradient of energy $E(s, u)$, $G$, is zero upon convergence and not the energy $E(s, u)$ itself. This would mean that CCMA system does not assemble properly or that the kinematic constraints are not satisfied. We solve this problem by adding the residual constraint energy $E_r = E(s, u)$ in the objective function $O$, where $0 < \lambda < 1$.

$$\min_{O(s(u), u)} \frac{1}{2}(X_{EE} - X_{EE}^*)^T (X_{EE} - X_{EE}^*) + \lambda \cdot E(s, u) \quad (2)$$

We also need to calculate the derivatives of the objective function $O$, as in Eqn. 3 with respect to the control variables, in order to use gradient based optimization techniques.

$$\frac{dO}{du} = \frac{\partial O}{\partial X_{EE}} \cdot \frac{dX_{EE}}{ds} \cdot \frac{ds}{du} + \lambda \cdot \frac{dE_r}{du} \quad (3)$$

The analytical expression for $\frac{\partial O}{\partial X_{EE}} \cdot \frac{dX_{EE}}{ds}$ is easily obtained. However, the expression for $\frac{dE_r}{du}$ is not generally analytically available and use of finite differences to compute it will require to minimize the constraint energy function $E(s, u)$ 2k times to high degree of accuracy, where $k$ is the size of the control vector $u$. This is computationally too demanding for a real time simulation and control tool. We solve this problem by doing the sensitivity analysis over the gradient $\frac{dE}{ds}$ of the constraint energy function $E(s, u)$ rather than over the constraint vector $C$ itself as done in the paper [18]. This is done because constraints can not be assumed to be satisfied during the intermediate iterations of the optimization of the objective function $O$. On the other hand, the gradient $\frac{dE}{ds}$ of the constraint energy function is always equal to zero, when the optimization in Eqn. 1 converges. To express it more clearly for every control vector $u$, one can find a suitable $s$ such that gradient of the constraint energy function $E(s, u)$ is zero. Thus we have the following identity:

$$G = \frac{dE}{ds} = 0 \ \forall u \implies \frac{dG}{du} = 0 \quad (4)$$

Doing the sensitivity analysis over this gradient $G$ leads to the following equation:

$$\frac{\partial G}{\partial u} + \frac{\partial G}{\partial s} \cdot \frac{ds}{du} = 0 \implies \frac{ds}{du} = -\left(\frac{\partial G}{\partial s}\right)^{-1} \cdot \frac{\partial G}{\partial u} \quad (5)$$

$\frac{\partial G}{\partial u}$ is the Hessian of the constraint energy function $E(s, u)$, which we calculate analytically. $\frac{\partial G}{\partial s}$ is the sensitivity of the gradient $G$ with respect to control vector $u$, while state $s$ is kept constant. We analytically calculate this term $\frac{\partial G}{\partial u}$ as well. With the analytical expressions for $\frac{\partial G}{\partial s}$ and $\frac{\partial G}{\partial u}$, finally we can compute $\frac{ds}{du}$:

$$\left.\frac{dE}{ds}\right|_{s=\hat{s}} = 0 \text{ because } s = \hat{s} \text{ is solution to Eqn. 1} \text{ Eqn. 3 requires calculation of an additional term } \frac{dE_r}{du} \text{ which is done}$$
as follows:

\[
\frac{dE_r}{du} = \frac{\partial E}{\partial u} \bigg|_{s=\hat{s}} + \frac{\partial E}{\partial s} \bigg|_{s=\hat{s}} \cdot \frac{ds}{du} = \frac{\partial E}{\partial u} \bigg|_{s=\hat{s}}
\]

We calculate this term $\frac{\partial E}{\partial u}$, in the Eqn. 6 theoretically.

Substituting expression for $\frac{ds}{du}$ and $\frac{dE}{du}$ in Eqn. 3, we can calculate the gradient $\frac{dO}{du}$ of the objective function $O$. This gradient can then be used to update the control vector $u$ in the current step of the optimization problem as follows:

\[
u_{i+1} = u_i - H^{-1} \cdot \frac{dO}{du} \bigg|_{u=u_i}
\]

For exact Newton method, we need analytically expression for the derivative of the Hessian of $E(s,u)$ with respect to state $s$, which we don’t calculate. Instead, we approximate $H^{-1}$ using the BFGS quasi-Newton method.

C. Results on convergence and computational effort

While it is possible to directly calculate the final control vector $u$ for large changes in $X_{EE}$. It is advisable to do small steps both in end-effector position and orientation until we reach the desired $X_{EE}$ especially for actual hardware experiments. This leads to smoother motion of the CCMA system, in particular during end-effector rotations. Fig. 4 presents the computational effort, in time, which is required to achieve a small combined perturbation in the $X_{EE}$, 10 mm step size for translation and 0.005 radians step size for rotation. The convergence and computational effort is presented for different CCMA system examples across different designs, morphologies of the passive kinematic chain and different number, actuation schemes of the mobile agents. It can be observed that the computational effort is smallest for the 4-DOF CCMA system with 3 mobile agents and highest for 6-DOF CCMA system with 6 agents. It is advisable that, for each plot, a combined perturbation in $X_{EE}$ was solved.

IV. EXPERIMENTAL RESULTS

In this section, we present the fabricated prototypes for the 4-DOF CCMA system with two different actuation schemes. Furthermore, we demonstrate the kinematic control of fabricated prototypes using the optimization framework developed in previous section and describe experimental results.

In order to determine and track the position and orientation of the mobile bases, with respect to the world reference frame, a motion capture system comprising of 10 OptiTrack Prime 13 cameras was used. Fig. 5 shows the omnidirectional base used for proof of concept demonstrators in the paper. Each mobile base has 6 optical markers (Fig. 5(a)) which can be tracked with the motion capture system. Motion capture system sends the feedback for the actutal mobile base position and orientation in the world reference frame to the computer running the optimization. In order to wirelessly transmit the control signals to the mobile bases, for the control of the CCMA demonstrators, we use wireless transreceivers XBees from Digi International. Each mobile base is equipped on its back with an XBee (Fig. 5(b)). The computer running the optimization sends the control commands to a micro-controller via serial communication. This micro-controller has a transceiver XBee, which acts as the co-ordinator. The co-ordinator XBee broadcasts the control signals wirelessly to the respective XBees, in each mobile base.

The optimization framework, as described in Sec. III calculates the states of the mobile bases for desired end-effector motions. The state of each mobile base is then converted to the corresponding wheel speeds based on the difference between the set and the tracked state of the mobile base, using a PI (proportional integral) controller. Please refer to the standard mobile robot kinematics for Swedish wheels based omnidirectional mobile robot in this work [23]. It should be noted that the closed loop feedback PI controller is used to track the states of the mobile bases only. For the experimental results described hereafter, end-effector motion of the CCMA system is still obtained via feed-forwarding the computed mobile base states in an open loop.

A. Reduced actuation scheme

Fig. 7 shows the fabricated prototype of the 4-DOF CCMA system. It can translate along $x_g$, $y_g$, $z_g$ and rotate about $z_g$. Between the mobile base and the adjacent link, there is a rotary connection obtained by use of two concentric cylinders (Fig. 5(b)). Therefore, this particular prototype utilizes the reduced actuation scheme and 2-DOF in translation of the
Fig. 6: (a) Mobile base has a fixed bolted connection with the link adjacent to it. This is the fabrication strategy for complete actuation schemes. (b) Mobile base has a rotary connection with the link adjacent to it. This is the fabrication strategy for reduced actuation schemes.

Fig. 7: Fabricated prototype of 4-DOF CCMA system example from Fig. 2(a) with optical markers.

Fig. 8: The tracked and simulated motion of the end-effector with reduced actuation scheme (a) translation along \( y_g \) (b) along \( z_g \) (c) along \( x_g \) (d) rotation about \( z_g \).

mobile bases (size of control vector \( \mathbf{u} \) is 6) to manipulate the 4-DOF end-effector. For experiments with this prototype, the orientation of the mobile base is kept constant. Fig. 8 shows the sequential movement along each DOF of the end-effector with respect to time. Fig. 9 and Fig. 10 shows the corresponding motion of the mobile bases with respect to time and the ground plane \( (x_g - y_g) \), respectively. RMSE
Please refer to the accompanying video for results in simulation for the 4-DOF and 6-DOF CCMA system examples and experimental results demonstrating different kinds of motion for the two 4-DOF CCMA prototypes.

V. DISCUSSION, CONCLUSIONS AND FUTURE WORK

A. Discussion

Due to use of mobile bases, the robots presented in paper can be quite dexterous and have large workspaces. However, certain workspaces such as translation workspace along \( z_g \) can be limited by the design parameters, such as link lengths, in the passive kinematic chain. In future, we aim to do the design optimization of the CCMA system for certain prescribed workspaces. Since the CCMA system effectively includes closed loop kinematic chains, treatment of singularities especially parallel singularities would be added in the optimization framework. The multiple actuation schemes, over-actuation and increase in number of mobile bases would be exploited to provide potential solutions in the future work. As these systems are scaled, they are bound to exhibit a lot more flexibility and compliance which is not necessarily a bad outcome, as the compliance can be good for safety reasons, but its effects have to be studied and possibly included in the simulation framework for accurate prediction of the end-effector states. Addition of on-board
sensors like IMUs, cameras, lidars on top of the wheel encoder’s information would enable more freedom for the CCMA system to be operated without an external motion tracking system.

The current paper dealt with a class of robots rather than evaluating a particular design of robot for a particular application. With an application or task specific design optimization which covers range of performance criterion such as precision, stiffness, payload and workspace, the CCMA system could in future be applicable to wide range of logistics, field robotics and service robotics tasks. In this paper, CCMA system was limited to totally passive kinematic chains which might be limiting for the payload capacity and stiffness required for certain applications. However, apart from using mobile agents as actuators in the CCMA system, a small subset of passive joints in closed-loop kinematic chains of the CCMA system could be actuated. This increased control and actuation space has the potential to significantly increase the stiffness and payload capacity of the CCMA system.

B. Conclusions and future work

In this work, we have introduced a generalized concept of constrained collaborative mobile agents. These systems have the potential to be scalable and adaptable according to the different task requirements. We have presented a novel optimization framework using sensitivity analysis, which allows flexibility to test different designs, topologies of passive kinematic chain, different number of mobile agents and different actuation schemes. With results in simulation, proof of concept prototypes and experimental quantitative results, we have demonstrated the efficacy of the developed optimization tool for the simulation and kinematic control of such systems.

In this work, we presented robots actuated with omnidirectional mobile bases. In the future work, we aim to work with different mobile bases such as mobile bases with non-holonomic constraints or quadruped robots, which would lead to different instantiations of the CCMA concept.

References


