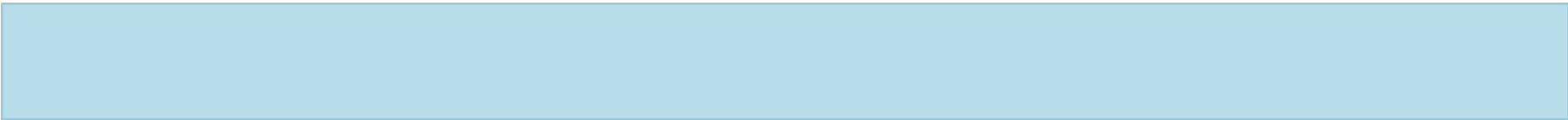


Lecture 13

# COMPILER DESIGN

# Announcements

- **HW 3:** due soon
- **HW 4:** Building a frontend
  - Work with lexer and parser generators
  - Compile a C-like source language to LLVM



Debugging parser conflicts.  
Disambiguating grammars.

# **MENHIR IN PRACTICE**

# Practical Issues

- Dealing with source file location information
  - In the lexer and parser
  - In the abstract syntax
  - See [range.ml](#), [ast.ml](#)
- Lexing comments/strings
  - See [lexer.mll](#)

# Menhir output

- You can get verbose ocaml yacc debugging information by doing
  - `menhir --explain ...`
  - or, if using ocamlbuild  
`ocamlbuild -use-menhir -yaccflag --explain ...`
- The result is a `<basename>.conflicts` file describing the error
  - The parser items of each state use the `'.'` just as described above
- The flag `--dump` generates a full description of the automaton
- Example: `start-parser.mly`

# Precedence and Associativity Declarations

- Parser generators often support precedence/associativity declarations
  - Hints to the parser about how to resolve conflicts
  - See [good-parser.mly](http://good-parser.mly)
- Pros
  - Avoids having to manually resolve those ambiguities by manually introducing extra nonterminals (as seen in [hand-parser.mly](http://hand-parser.mly))
  - Easier to maintain the grammar
- Cons
  - Can't as easily re-use the same terminal (if associativity differs)
  - Introduces another level of debugging
- Limits
  - Not always easy to disambiguate just with precedence/associativity

# Example Ambiguity in Real Languages

- Consider this grammar

$S \mapsto \text{if } (E) S$

$S \mapsto \text{if } (E) S \text{ else } S$

$S \mapsto X = E$

$E \mapsto \dots$

- Is this grammar OK?

- Consider how to parse

$\text{if } (E_1) \text{ if } (E_2) S_1 \text{ else } S_2$

- The “dangling else” problem
- Which is the “right” answer?
- How to change the grammar?

# How to disambiguate if-then-else

- Want to rule out

$$\text{if } (E_1) \left\{ \text{if } (E_2) S_1 \right\} \text{ else } S_2$$

- Observation: An un-matched 'if' should not appear as the 'then' clause of a containing 'if'

```
S  $\mapsto$  M | U // M = "matched", U = "unmatched"  
U  $\mapsto$  if (E) S // Unmatched 'if'  
U  $\mapsto$  if (E) M else U // Nested if is matched  
M  $\mapsto$  if (E) M else M // Matched 'if'  
M  $\mapsto$  X = E // Other statements
```

- See [else-resolved-parser.mly](#)



# Alternative: Use { }

- Ambiguity arises because the 'then' branch is not well bracketed

```
if (E1) { if (E2) { S1 } } else S2 // unambiguous
if (E1) { if (E2) { S1 } else S2 } // unambiguous
```

- So, one could just require brackets
  - But requiring them for the else clause too leads to ugly code for chained if-statements

```
if (c1) {
  ...
} else {
  if (c2) {
  } else {
    if (c3) {
    } else {
    }
  }
}
```

So, compromise? Allow unbracketed else block only if the body is 'if'

```
if (c1) {
} else if (c2) {
} else if (c3) {
} else {
}
```

## Benefits

- Less ambiguous
- Easy to parse
- Enforces good style



See HW4

**OAT V 1.0**

# OAT

- Simple C-like imperative language
  - Supports 64-bit integers, arrays, strings
  - Top-level, mutually recursive procedures
  - Scoped local, imperative variables
- See examples in HW#4 later
- How to design/specify such a language?
  - Grammatical constructs
  - Semantic constructs

# Compilation in a Nutshell

Source Code

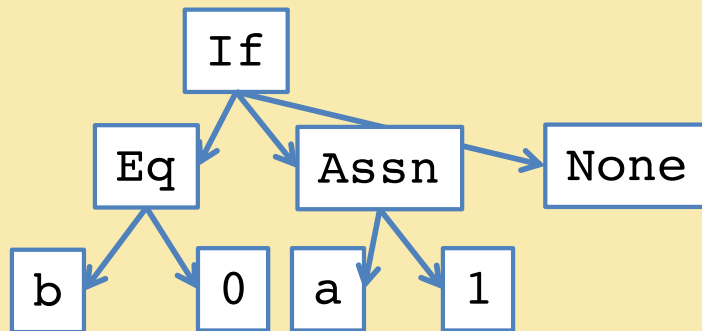
(Character stream)

```
if (b == 0) { a = 1; }
```

Token stream:

if	(	b	==	0	)	{	a	=	0	;	}
----	---	---	----	---	---	---	---	---	---	---	---

Abstract Syntax Tree:



Intermediate code:

```
11: %cnd = icmp eq i64 %b, 0
    br i1 %cnd, label %12, label %13
12: store i64* %a, 1
    br label %13
13:
```

Assembly Code

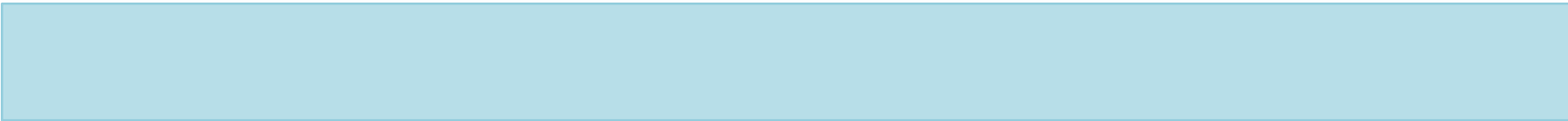
```
11: cmpq %eax, $0
    jeq 12
    jmp 13
12:
...
```

Lexical Analysis

Parsing

Analysis & Transformation

Backend



Untyped lambda calculus  
Substitution  
Evaluation

# FIRST-CLASS FUNCTIONS

# “Functional” languages

- Languages like ML, Haskell, Scheme, Python, C#, Java 8, Swift
  - Functions can be passed as arguments (e.g. map or fold)
  - Functions can be returned as values (e.g. compose)
  - **Function nest:**
    - Inner function can refer to variables bound in the outer function

```
let add = fun x -> fun y -> x + y
```

```
let inc = add 1
```

```
let dec = add -1
```

```
let compose = fun f -> fun g -> fun x -> f (g x)
```

```
let id = compose inc dec
```

- How do we implement such functions?
  - In an interpreter? In a compiled language?

# (Untyped) Lambda Calculus

- The lambda calculus is a minimal programming language
  - Note: we're writing `(fun x -> e)` lambda-calculus notation:  $\lambda x. e$
- It has variables, functions, and function application
  - That's it!
  - It's Turing Complete
  - It's the foundation for a *lot* of research in programming languages
  - Basis for “functional” languages like Scheme, ML, Haskell, etc.

Abstract syntax in OCaml

```
type exp =  
  | Var of var          (* variables          *)  
  | Fun of var * exp    (* functions: fun x -> e *)  
  | App of exp * exp    (* function application *)
```

Concrete syntax

```
exp ::=  
  | x          variables  
  | fun x -> exp functions  
  | exp1 exp2 function application  
  | ( exp )    parentheses
```

# Values and Substitution

- The only values of the lambda calculus are (closed) functions

```
val ::=  
    | fun x -> exp    functions are values
```

- To *substitute* value  $v$  for variable  $x$  in expression  $e$ 
  - Replace all *free occurrences* of  $x$  in  $e$  by  $v$
  - In OCaml: written `subst v x e`
  - In Math: written  $e\{v/x\}$

- Function application is interpreted by *substitution*

```
(fun x -> fun y -> x + y) 1  
= subst 1 x (fun y -> x + y)  
= (fun y -> 1 + y)
```



# Lambda Calculus Operational Semantics

- Substitution function (in Math)

$x\{v/x\}$	$= v$	<i>(replace the free x by v)</i>
$y\{v/x\}$	$= y$	<i>(assuming <math>y \neq x</math>)</i>
$(\text{fun } x \rightarrow \text{exp})\{v/x\}$	$= (\text{fun } x \rightarrow \text{exp})$	<i>(x is bound in exp)</i>
$(\text{fun } y \rightarrow \text{exp})\{v/x\}$	$= (\text{fun } y \rightarrow \text{exp}\{v/x\})$	<i>(assuming <math>y \neq x</math>)</i>
$(e_1 e_2)\{v/x\}$	$= (e_1\{v/x\} e_2\{v/x\})$	<i>(substitute everywhere)</i>

- Examples

$$x y \{(\text{fun } z \rightarrow z)/y\} \Rightarrow x (\text{fun } z \rightarrow z)$$

$$(\text{fun } x \rightarrow x y)\{(\text{fun } z \rightarrow z) / y\} \Rightarrow (\text{fun } x \rightarrow x (\text{fun } z \rightarrow z))$$

$$(\text{fun } x \rightarrow x)\{(\text{fun } z \rightarrow z) / x\} \Rightarrow (\text{fun } x \rightarrow x) \quad // x \text{ is not free!}$$

# Free Variables and Scoping

```
let add = fun x -> fun y -> x + y
let inc = add 1
```

- The result of `add 1` is a function
- After calling `add`, we can't throw away its argument (or its local variables) because those are needed in the function returned by `add`
- We say variable `x` is *free* in `fun y -> x + y`
  - Free variables are defined in an outer scope
- We say variable `y` is *bound* by “`fun y`”
  - Its scope is the body “`x + y`” in `fun y -> x + y`
- A term with no free variables is called *closed*
- A term with one or more free variables is called *open*

# Free Variable Calculation

- OCaml code to compute the set of free variables in lambda expressions

```
let rec free_vars (e:exp) : VarSet.t =
  begin match e with
    | Var x          -> VarSet.singleton x
    | Fun(x, body)  -> VarSet.remove x (free_vars body)
    | App(e1, e2)   -> VarSet.union (free_vars e1) (free_vars e2)
  end
```

- Lambda expression  $e$  is *closed* if `free_vars e` is `VarSet.empty`
- In math notation

$$\begin{aligned} \text{fv}(x) &= \{x\} \\ \text{fv}(\text{fun } x \text{ -> } \text{exp}) &= \text{fv}(\text{exp}) \setminus \{x\} \quad ('x' \text{ is a bound in } \text{exp}) \\ \text{fv}(\text{exp}_1 \text{ exp}_2) &= \text{fv}(\text{exp}_1) \cup \text{fv}(\text{exp}_2) \end{aligned}$$

# Variable Capture

- Note that if we try to naively "substitute" an open term, a bound variable might **capture** the free variables

$$= \text{fun } x \rightarrow (x \text{ (fun } z \rightarrow x))$$

Note:  $x$  is free in  $(\text{fun } z \rightarrow x)$   
free  $x$  is *captured!!*

- Usually *not* the desired behavior
  - This property is sometimes called "dynamic scoping"

The meaning of " $x$ " is determined by where it is bound dynamically (not where it is bound statically)

- Some languages (e.g. Emacs Lisp) are implemented with this as a "feature"
- But, leads to hard to debug scoping issues

# Alpha Equivalence

- Note that the names of bound variables don't matter

(fun x -> y x) the "same" as (fun z -> y z)

- Two terms that differ only by consistent renaming of bound variables are called alpha equivalent
- The names of free variables do matter

(fun x -> y x) *not* the "same" as (fun x -> z x)

Intuitively: y and z may refer to different things from some outer scope

# Fixing Substitution

- Consider the substitution operation

$$e_1\{e_2/x\}$$

- To avoid capture, define substitution to pick an alpha equivalent version of  $e_1$  such that the bound names of  $e_1$  don't mention the free names of  $e_2$
- Then do the "naïve" substitution

- Example

$$\begin{aligned} & (\text{fun } x \text{ -> } (x \ y)) \{(\text{fun } z \text{ -> } x) / y\} \\ = & (\text{fun } x' \text{ -> } (x' \ (\text{fun } z \text{ -> } x))) \quad \textit{rename } x \text{ to } x' \end{aligned}$$

# Operational Semantics

- Specified with 2 inference rules with judgments of the form  $\text{exp} \Downarrow v$ 
  - Read this notation as “program  $\text{exp}$  evaluates to value  $v$ ”
  - We give a *call-by-value* semantics
    - Function arguments are evaluated before substitution

$$\frac{}{v \Downarrow v}$$

“Values evaluate to themselves”

$$\frac{\text{exp}_1 \Downarrow (\text{fun } x \rightarrow \text{exp}_3) \quad \text{exp}_2 \Downarrow v \quad \text{exp}_3\{v/x\} \Downarrow w}{\text{exp}_1 \text{ exp}_2 \Downarrow w}$$

“To evaluate function application: Evaluate the function to a value, evaluate the argument to a value, and then substitute the argument for the function. ”



See [fun.ml](#)

# IMPLEMENTING THE INTERPRETER