8th Homework

- In this homework, we shall model and simulate a mechanical system as well as exercise the state selection algorithm.
- We shall first model a car bumping into a wall using the 1D mechanical (translational) wrapped bond graph library.
- We shall then model the same car using a bond graph directly.
- Subsequently, we shall read out the model equations from the bond graph.
- Finally, we shall change one of the state variables using the state selection algorithm.



- Model description
- <u>1D mechanical wrapped bond graph model</u>
- Direct bond graph model
- <u>State selection</u>



Mechanical System

• We wish to analyze the following system:



November 8, 2012

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Mechanical System II

- Questions of interest:
 - Are the shock absorbers (k_2, B_2) and the safety belts (k_1, B_1) capable of preventing the driver from hitting his head on the front windshield if he drives with a velocity of 40 km/h against a solid wall? What happens when the velocity at impact is 80 km/h?
 - How large is the maximal force that the driver experiences at these velocities?
 - How large is the critical velocity, below which the driver neither hits his head on the windshield, nor breaks his ribs?



Mechanical System III

• Data:

Mass of vehicle (M) = 1500 kgMass of driver (m) = 100 kgStiffness of safety belt $(k_1) = 10'000 \text{ N/m}$ Stiffness of shock absorber $(k_2) = 300'000 \text{ N/m}$ Damping of safety belt $(B_1) = 500 \text{ Ns/m}$ Damping of shock absorber $(B_2) = 80'000 \text{ Ns/m}$

• Limit values:

Safety belt tested up to $(F_1) < 13'340$ N Ribs break beyond $(F_2) > 6670$ N Distance to windshield (d) = 0.5 m



Mechanical System IV

- Model the car and the driver using two sliding masses of the translational sub-library of the mechanical sub-library of *BondLib*.
- Simulate the system across *0.5 sec* of simulated time, and answer the questions that were raised before.



Mechanical System V

- Draw a bond graph of this system.
- Simplify the bond graph using the diamond property.
- Add causality strokes.
- Simulate the simplified bond graph model using *BondLib*, and compare the results with those obtained earlier.



Mechanical System VI

- Read the model equations out of the simplified bond graph.
- What is the model order?
- Which are the natural state variables?
- We now wish to include the relative position and the relative velocity of the spring representing the seat belt among the set of desired state variables.
- Use the state selection algorithm to derive a modified set of equations that make use of the desired state variables.

