Eifigenössische Technische Mochschule Zühlch Swiss. Rederall Institute of Technologg Zuhlch	Mathematical Modeling of Physical Systems
3D Mechanics	
	ow look at a second application of graphs: <i>3D mechanics</i> .
planar mecl	cal models look superficially just like nanical models. There are additional nts, but other than that, there seem to rises.
deceiving. complicatio	seemingly similar appearance is There are a substantial number of ns that the modeler has to cope with ag with 3D mechanics. These are the is lecture.
November 15, 2012	© Prof. Dr. François E. Cellier







Cidgenössische Technische Hochschule Zünich Sidgenössische Technische Hochschule Zünich Swiss. Rederal Institutie af Technology Zunich

Mathematical Modeling of Physical Systems

3D Mechanical Connectors

• The 3D mechanical multi-bond connectors should carry 13 variables, an effort vector, **e**, of length 6, a flow vector, **f**, also of length 6, plus the directional variable, *d*.



公

- The 3D mechanical multi-body connectors would need to carry 18 variables, namely 12 potential variables describing the 6 generalized positions and the 6 generalized velocities, and 6 flow variables describing the generalized forces.
- In reality, they carry 24 variables, as shown on the next slide.

November 15, 2012

© Prof. Dr. François E. Cellier Start Presentation



ETH Mathematical Modeling of Physical Systems Eidgenössische Technische Hochschule Zünich Swiss. Referall Institute of Technology Zunich The Body-fixed Coordinate System • In 3D mechanics, the inertial tensor depends on the orientation of the body relative to its coordinate system. • Hence, if the *world coordinate system* is being used for formulating the d'Alembert principle for rotational motion, the inertial tensor must be constantly updated. • Alternatively, we can formulate the d'Alembert principle in a body-fixed coordinate system. In this way, the inertial tensor remains constant. • However, we now must calculate the relative coordinate transformations across joints. • We must also take into account the *gyroscopic torques* that result from formulating the d'Alembert principle in an accelerated frame. November 15, 2012 Start Presentation $\langle \downarrow \rangle$ © Prof. Dr. François E. Cellier

ETH Eidgen össische Technische Hochschule Zühich Gwiss. Endered Institute of Technology Zunich

Mathematical Modeling of Physical Systems

The Body-fixed Coordinate System II

- In planar mechanics, this wasn't a problem yet. There is a single axis of rotation that is always perpendicular to the plane of translation.
- Consequently, the inertia remains constant, and we can (and have been) calculating all motions in the world coordinate system.
- This fact makes planar mechanics considerably simpler and more easy to understand than 3D mechanics.

```
November 15, 2012
```

© Prof. Dr. François E. Cellier Start Presentation

公众



























Rotational multibond graph

© Prof. Dr. François E. Cellier

Start Presentation

公众

November 15, 2012



















