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Mathematical Modeling of Physical Systems

Object Oriented Modeling

- The aim of this lecture is to illustrate the requirements of a *software environment* for *object-oriented modeling of physical systems* and to show how these requirements can be met in practice.
- The lecture offers a first glimpse at features and capabilities of *Dymola*, a software environment created for the purpose of modeling complex physical systems in an object-oriented fashion. *Dymola* offers a *graphical user interface*.
- Some features of the underlying textual model representation, called *Modelica*, are also introduced.

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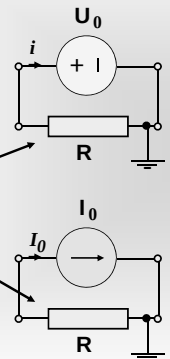


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The Causality of the Model Equations

Identical Objects



Different Equations

$$U_0 = f(t)$$

$$i = U_0 / R$$

$$I_0 = f(t)$$

$$u = R \cdot I_0$$

⇒ The causality of the equations must not be predetermined. It can only be decided upon after the analysis of the system topology.

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Basic Requirements of OO Modeling

- Physical objects should be representable by mathematical graphical objects.
- The graphical objects should be *topologically* connectable.
- The mathematical models should be *hierarchically* describable. To this end, it must be possible to represent networks of coupled objects again as graphical objects.

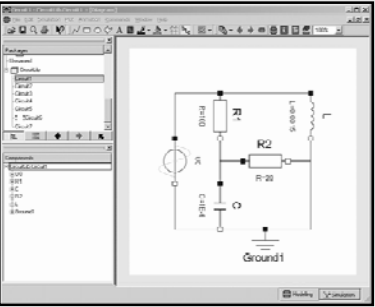
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An Example



Dymola

```

model Circuit1
  SineVoltage U0(V=10, freqHz=2500);
  Resistor R1(R=100);
  Resistor R2(R=20);
  Capacitor C(C=1E-6);
  Inductor L(L=0.0015);
  Ground Ground;
equation
  connect(U0.p, R1.p);
  connect(R1.n, C.p);
  connect(R2.p, R1.n);
  connect(U0.n, C.n);
  connect(Ground.p, C.n);
  connect(L.p, R1.p);
  connect(L.n, Ground.p);
  connect(R2.n, L.n);
end Circuit1;

```

Modelica

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Graphical Information (Annotation)

```

package CircuitLib
  annotation (Coordsys( extent=[0, 0; 504, 364], grid=[2, 2], component=[20, 20]));
  model Circuit1
    annotation (Coordsys( extent=[-100, -100; 100, 100], grid=[2, 2], component=[20, 20]));
    Modelica.Electrical.Analog.Sources.SineVoltage U0(V=10, freqHz=2500)
      annotation (extent=[-80, -20; -40, 20], rotation=-90);
    Modelica.Electrical.Analog.Basic.Resistor R1(R=100) annotation (extent=[-40, 20; 0, 60], rotation=-90);
    Modelica.Electrical.Analog.Basic.Capacitor C(C=1E-6) annotation (extent=[-40, -60; 0, -20], rotation=-90);
    Modelica.Electrical.Analog.Basic.Resistor R2(R=20) annotation (extent=[0, -20; 40, 20]);
    Modelica.Electrical.Analog.Basic.Inductor L(L=0.0015) annotation (extent=[40, 20; 80, 60], rotation=-90);
    Modelica.Electrical.Analog.Basic.Ground Ground annotation (extent=[0, -100; 40, -60]);
  equation
    connect(U0.p, R1.p) annotation (points=[-60, 20; -60, 60], style(color=3));
    connect(R1.n, C.p) annotation (points=[-20, 20; -20, -20], style(color=3));
    connect(R2.p, R1.n) annotation (points=[0, -20; -20, 20], style(color=3));
    connect(U0.n, C.n) annotation (points=[-60, -20; -60, -60], style(color=3));
    connect(Ground.p, C.n) annotation (points=[20, -60; -20, -60], style(color=3));
    connect(L.p, R1.p) annotation (points=[60, 60; -20, 60], style(color=3));
    connect(L.n, Ground.p) annotation (points=[60, 20; 60, -60], style(color=3));
    connect(R2.n, L.n) annotation (points=[40, 0; 60, 20], style(color=3));
  end Circuit1;
end CircuitLib;

```

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Models in Modelica

- Models in *Modelica* consist of a description of their *model structure* as well as a description of their *embedding in the model environment*:

```

model Model name
  Description of the model embedding;
equation
  Description of the model structure;
end Model name;

```

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Model Structure in Modelica

- The model structure in *Modelica* consists either of a set of equations, a description of the model topology, or a combination of the two types of model structure descriptions.
- A topological model description is usually done by dragging and dropping model icons from graphical model libraries into the modeling window. These models are then graphically interconnected among each other.
- The stored textual version of the topological model consists of a declaration of its sub-models (model embedding), a declaration of its connections (model structure), as well as a declaration of the graphical description elements (annotation).

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Model Topology in Modelica

model MotorDrive

Class name

Motor

Gearbox

Shaft

Tachometer

equation

connect(controller.out, motor.inp);

connect(motor.flange, gearbox.a);

connect(gearbox.b, J1.a);

connect(J1.b, wl.a);

connect(wl.w, controller.inp);

end MotorDrive;

Connection

Instance name

controller;

motor;

gearbox(n=100);

J1(J=10);

Modifier

Connector

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Resistors in Modelica

```

model Resistor "Ideal resistor"
  Pin p, n;
  Voltage u;
  parameter Resistance R;
  equation
    u = p.v - n.v;
    p.i + n.i = 0;
    R*p.i = u;
  end Resistor;
  
```

connector Pin

Voltage v;

flow Current i;

end Pin;

type ElectricPotential = Real
(final quantity="ElectricPotential",
final unit="V");

type Voltage = ElectricPotential;

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Similarity Between Different Elements

```

model Resistor "Ideal resistor"
  Pin p, n;
  Voltage u;
  parameter Resistance R;
  equation
    u = p.v - n.v;
    p.i + n.i = 0;
    R*p.i = u;
  end Resistor;
  
```

```

model Capacitor "Ideal capacitor"
  Pin p, n;
  Voltage u;
  parameter Capacitance C;
  equation
    u = p.v - n.v;
    p.i + n.i = 0;
    C*der(u) = p.i;
  end Capacitor;
  
```

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Partial Models and Inheritance

```

partial model OnePort
  Pin p, n;
  Voltage u;
  equation
    u = p.v - n.v;
    p.i + n.i = 0;
  end OnePort;

  model Resistor "Ideal resistor"
    extends OnePort;
    parameter Resistance R;
    equation
      R*p.i = u;
  end Resistor;

  model Capacitor "Ideal capacitor"
    extends OnePort;
    parameter Capacitance C;
    equation
      C*der(u) = p.i;
  end Capacitor;
  
```

```

model Capacitor "Ideal capacitor"
  Pin p, n;
  Voltage u;
  parameter Capacitance C;
  equation
    C*der(u) = p.i;
  end Capacitor;
  
```

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Decomposition and Abstraction

Courtesy Toyota Tera-Service

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Heterogeneous Modeling Formalisms

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Simulation and Animation

Modeling Window

Animation Window

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